SPC based software reliability using Modified Genetic Algorithm: GO model

Dr. R. Satyaprasad, U. Usha Rani, Dr. G. Krishna Mohan
Assoc. Professor, Dept. of CSE, Acharya Nagarjuna University. Research Scholar, Rayalaseema University. Professor, Dept. of CSE, KL University, Vaddeswaram.

Abstract— To assess software reliability, many software reliability growth models (SRGMs) have been proposed in the past four decades. In principle, two widely used methods for the parameter estimation of SRGMs are the maximum likelihood estimation (MLE) and the least squares estimation (LSE). However, the approach of these two estimations may impose some restrictions on SRGMs, such as the existence of derivatives from formulated models or the needs for complex calculation. In this paper, a Modified Genetic Algorithm (MGA) with Statistical Process Control (SPC) is proposed to assess the reliability of software considering the Time domain software failure data using Goel-Okumoto (GO) model which is NonHomogenous Poisson Process (NHPP) based. Experiments based on real software failure data are performed, and the results show that the proposed genetic algorithm is more effective and faster than traditional algorithms.

Keywords - Software reliability, GO model, Time domain data, Mean Value Function, Modified Genetic Algorithm, SPC, NHPP.

I. INTRODUCTION.

One of the most difficult problems of software industry is to ship a reliable product. Therefore it is necessary to have accurate and fast estimation techniques for verifying software reliability. Software reliability assessment is important to evaluate the quality of software system, since it is one of the most important attribute of software. For Four decades, many Software Reliability Growth Models (SRGMs) have been proposed in estimating reliability growth of software products. SRGMs can be used to depict the behaviour of observed software failures characterized by either times of failures (i.e Time domain data) or by the number of failures at fixed times (i.e Interval domain data) (Lyu, 1996).

The parameters of SRGMs are generally unknown and have to be estimated based on collected failure data. Two of the most popular estimation techniques are Maximum Likelihood Estimation (MLE) and Least Squares Estimation (LSE) (Goel, 1985; Ohba, 1984). In fact, MLE and LSE involve the property of probability theory and statistical analysis. Thus, this may impose some restrictions on the parameter estimation of SRGMs (Costa et al., 2007; Minohara and
such as the continuity, the unimodality, the existence of derivatives from formulated models, the complex likelihood function, etc. The method of MLE estimation by solving a set of simultaneous equations and is better in deriving confidence intervals. The method of LSE minimizes the sum of squares of the deviations between what we actually observe and what we expect. Nevertheless, LSE is suitable for fitting data from small to medium sample sizes (Wood, 1996), while MLE is considered to be better statistical estimator for large sample sizes. In particular, when the formulated model of SRGMs is complicated or the sample size of failure data is large, these two estimation techniques may not be effective to find out the optimal solutions and generally require to be solved numerically. Hence, the more effective and applicable approaches for the parameter estimation of SRGMs may be necessary.

In recent years, the Genetic Algorithms (GAs) has gained popularity in solving the optimization problem of scientific fields (Goldberg, 1989 ; Mitchell, 1998). Because, the parameter estimation can be reformulated as a searching process within the domain of all the feasible solutions (Harman and Jones, 2001; Jiang, 2006), it may be attractive to introduce GA into the process of software reliability modeling (Dai et al., 2003). Therefore, in this paper we will propose a modified genetic algorithm (MGA) to estimate the parameter of the SRGMs. We will attempt to modify GA’s operators with weighted bit mutation and a rebuilding mechanism to improve the performance and efficiency of estimations. Finally, the applicability of proposed MGA, the result of parameter estimation and the reliability with GO model will also be demonstrated through real data.

The rest of this paper is organized as follows. Section 2 surveys NHPP based SRGMs and in specific GO Model along with the past researches of GAs in software engineering areas. In Section 3, an effective MGA is proposed to solve the parameter estimation of reliability models. Then, the experimental results based on two failure data are presented and discussed in Section 4. Finally, some conclusions are given in Section 5.

II. LITERATURE SURVEY.

A. NHPP model.

The Non-Homogenous Poisson Process (NHPP) based software reliability growth models (SRGMs) are proved to be quite successful in practical software reliability engineering (Musa et al., 1987). The main issue in the NHPP model is to determine an appropriate mean value function to denote the expected number of failures experienced up to a certain time point. Model parameters can be estimated by using Modified Genetic
Algorithm (MGA). Various NHPP SRGMs have been built upon various assumptions. Many of the SRGMs assume that each time a failure occurs, the fault that caused it can be immediately removed and no new faults are introduced. Which is usually called perfect debugging. Imperfect debugging models have proposed a relaxation of the above assumption (Pham, 1993).

A fault is a statement in a program which causes one or more failures. Software Reliability Growth is defined by the mathematical relationship that exists between the time span of testing a program and the cumulative number of errors discovered. After failure detection, we find a fault and define a fix for the fault. The exponential software reliability growth models are designed to describe the failure detection process.

Let \( \{N(t), t \geq 0\} \) be the cumulative number of software failures by time ‘t’. \( m(t) \) is the mean value function, representing the expected number of software failures by time ‘t’. \( \lambda(t) \) is the failure intensity function, which is proportional to the residual fault content. Thus
\[
m(t) = a \left(1 - e^{-bt}\right) \quad \text{and} \quad \lambda(t) = \frac{dm(t)}{dt}.
\]
where ‘a’ denotes the initial number of faults contained in a program and ‘b’ represents the fault detection rate. In software reliability, the initial number of faults and the fault detection rate are always unknown. The maximum likelihood technique can be used to evaluate the unknown parameters. This paper deals with the application of GO model on application test data collected from literature, which is of Time domain data (i.e ungrouped).

SRGMs are a statistical interpolation of defect detection data by mathematical functions. They have been grouped into two classes of models- Concave and S-shaped. The only way to verify and validate the software is by testing. This involves running the software and checking for unexpected behaviour of the software output (kapur, 2009). SRGMs are used to estimate the reliability of a software product. In literature, we have several SRGMs developed to monitor the reliability growth during the testing phase of the software development. Software reliability is defined as the probability of failure-free software operation for specified period of time ‘t’ in a specified environment.

B. GO Model.

The Goel-Okumoto model is a simple Non-Homogenous Poisson Process (NHPP) model with the mean value function
\[
m(t) = a \left(1 - e^{-bt}\right) \quad \text{and} \quad \lambda(t) = abe^{-bt}.
\]

Where the parameter ‘a’ is the number of initial faults in the software and the parameter ‘b’ is the fault detection rate. The corresponding failure intensity function is given by \( \lambda(t) = abe^{-bt} \).
Assumptions:

- From the failure detection point of view, all faults in a program are mutually independent.
- The number of failures at any time is proportional to the current number of faults in a program.
- The probability of failure detection is constant.
- The isolated faults are removed prior to future test occasions.

C. Statistical Process Control

SPC concepts and methods are used to monitor the performance of a software process over time in order to verify that the process remains in the state of statistical control. It helps in finding assignable causes, long term improvements in the software process. Software quality and reliability can be achieved by eliminating the causes or improving the software process or its operating procedures (Kimura, 1995).

The most popular technique for maintaining process control is control charting. Software process control is used to secure, that the quality of the final product will conform to predefined standards. In any process, regardless of how carefully it is maintained, a certain amount of natural variability will always exist. A process is said to be statistically “in-control” when it operates with only chance causes of variation. On the other hand, when assignable causes are present, then we say that the process is statistically “out-of-control”. The control charts can be classified into several categories, according to several distinct criteria. Control charts should be capable to create an alarm when a shift in the level of one or more parameters of the underlying distribution occurs or a non-random behavior comes into. Normally, such a situation will be reflected in the control chart by points plotted outside the control limits or by the presence of specific patterns. For a process to be in control the control chart should not have any trend or nonrandom pattern.

SPC provides real time analysis to establish controllable process baselines; learn, set, and dynamically improve process capabilities; and focus business areas needing improvement. The early detection of software failures will improve the software reliability. The selection of proper SPC charts is essential to effective statistical process control implementation and use. The SPC chart selection is based on data, situation and need. Many factors influence the process, resulting in variability. The causes of process variability can be broadly classified into two categories, viz., assignable causes and chance causes.

The control limits can then be utilized to monitor the failure times of components. After each failure, the time can be plotted on
the chart. If the plotted point falls between the calculated control limits, it indicates that the process is in the state of statistical control and no action is warranted. If the point falls above the UCL, it indicates that the process average, or the failure occurrence rate, may have decreased which resulted in an increase in the item between failures. This is an important indication of possible process improvement. If this happens, the management should look for possible causes for this improvement and if the causes are discovered then action should be taken to maintain them. If the plotted point falls below the LCL, it indicates that the process average, or the failure occurrence rate, may have increased which resulted in a decrease in the failure time. This means that process may have deteriorated and thus actions should be taken to identify and remove them.

### III. MODIFIED GENETIC ALGORITHM.

Genetic Algorithm (GA) has been popularly used to solve various optimization problems. GA has advantages of easy implementation with large search space and rapid convergence on good quality solutions. It does not impose restrictions on the continuity, the existence of derivatives, and the unimodality of evaluation functions. Traditional GA has several steps for searching process:

- **chromosome representation;**

GA simulates the initial population of parametric solution represented as chromosomes. Each chromosome is encoded as a string of bits. Since the parameters of SRGMs are usually real numbers, we proposed an IEEE floating-point standard to encode chromosomes.

- **fitness function;**
  - **least squares estimation (LSE)**

\[
\text{fitness}_{\text{LSE}} = \frac{1}{\text{MSE}}
\]
Where, MSE is a measure to compare the differences between actual values and estimators.

- **Selection scheme:** This scheme is to select the candidate chromosomes from the current population based on their fitness values. Our goal is to maximize fitness function for finding the best parameters. With these fitness values, we can further adopt roulette wheel selection and uniform crossover to choose candidate chromosomes. A rebuilding mechanism is proposed. Among each generation, one best chromosome is kept at the end of the population to avoid disappearance from the selection scheme. This mechanism does not violate GA’s original purpose.

- **Crossover operator:** Two chromosomes are chosen from the population and are exchanged in part with each other in order to improve their fitness value. The uniform crossover is one of the simplest forms (Goldberg, 1989). The crossover may happen at different bits with a probability called crossover rate, P. This rate typically ranges from 0.5 to 0.8 from GA literatures (Jiang, 2006). It is decide to adopt uniform crossover in our experiments.

- **Mutation operator:** In IEEE floating-point format, it is found that some bits are less efficient during bit mutation. The sign bit mutation is useless as the estimated parameter are a positive real numbers. Similarly, if we mutate at a very high exponential bit or at a very low fractional bit, the whole string will respectively be \(2^{\pm128}\) times the original or only be changed slightly. In fact, these mutations may be too severe or negligible. Depending on Sensitivity analysis on different bit mutations, a weighted bit mutation is provided.

- **Stopping criteria:** The searching process will iteratively evolve parametric solutions until the maximal generations equal to 10000 trials or the best fitness function does not change in the past 10000 trials.

### A. Algorithm for parameter estimation

In this section, we show how to modify the traditional GA to estimate the parameters of SRGMs. The detailed algorithm of MGA is shown below. It is noted that all the proposed mechanisms of MGA are built by using Java programming language.

1. Initialize a population of chromosomes randomly
2. FOR (Iteration i=1; i<=Maximum generation && termination condition=FALSE; i=i+1)
   a. Calculate fitness for all individual chromosomes
   b. Reproduce offspring by roulette selection
   c. Choose two chromosomes from the population in order and randomize a probability p
   d. IF p < Crossover rate THEN
      i. Generate two offsprings by recombining two chromosomes.
   ENDIF
   e. Choose a chromosome from the population in order and randomize a probability q
   f. IF q < Mutation rate THEN
      i. Mutate the chosen chromosome at a weighted bit position
   ENDIF
   g. Keep the fittest parent in the end of population
   h. Check termination condition
3. ENDFOR
4. Output estimated parameters

IV. ILLUSTRATING THE MGA.
   A. Data Analysis.

There are two common types of failure data: time-domain and interval-domain. Some software reliability models can handle both types of data. The time domain approach involves recording the individual times at which failure occurred. The interval domain approach is characterized by counting the number of failures occurring during a fixed period (e.g., test session, hour, week, day). The collected data is the Time Between Failures. Based on the failure data collected from the literature, we used cumulative failures data for software reliability using GO model.

   B. Distribution of Time between failures

Based on the inter failure data given in Table 2 and 3, we compute the software failures process through Failure Control chart. We used cumulative time between failures data for software reliability monitoring using GO model. The use of cumulative quality is a different and new approach, which is of particular advantage in reliability.

‘\( \hat{a} \)’ and ‘\( \hat{b} \)’ are Maximum Likelihood Estimates of parameters and the values can be computed using iterative method for the given cumulative time between failures data. Using ‘\( a \)’ and ‘\( b \)’ values we can compute \( m(t) \).

Assuming an acceptable probability of false alarm of 0.27%, the control limits can be obtained as (Xie, 2002):

\[
T_U = 1 - e^{-(\hat{b})} = 0.99865
\]

\[
T_C = 1 - e^{-(\hat{b})} = 0.5
\]
\[ T_L = 1 - e^{-bt} = 0.00135 \]

These limits are converted to \( m(t_c), m(t_e) \) and \( m(t_L) \) form. They are used to find whether the software process is in control or not by placing the points in Failure control shown in figure 1 and 2. A point below the control limit \( m(t_L) \) indicates an alarming signal. A point above the control limit \( m(t_y) \) indicates better quality. If the points are falling within the control limits, it indicates the software process is in stable condition. The values of control limits are as follows.

**TABLE I. Estimated parameters and control limits**

<table>
<thead>
<tr>
<th>Data Set</th>
<th>Parameters</th>
<th>Control limits</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>a</td>
<td>b</td>
</tr>
<tr>
<td>DS1 (NTDS)</td>
<td>95.382252</td>
<td>0.075794</td>
</tr>
<tr>
<td>DS2 (IBM)</td>
<td>99.447446</td>
<td>0.019155</td>
</tr>
</tbody>
</table>

**TABLE II. DS1 - Successive differences of mean value function**

<table>
<thead>
<tr>
<th>Failure Number</th>
<th>Time Between failures</th>
<th>m(t)</th>
<th>Successive Differences</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>9</td>
<td>47.163571</td>
<td>28.800331</td>
</tr>
<tr>
<td>2</td>
<td>21</td>
<td>75.963901</td>
<td>10.982551</td>
</tr>
<tr>
<td>3</td>
<td>32</td>
<td>86.946452</td>
<td>2.206222</td>
</tr>
<tr>
<td>4</td>
<td>36</td>
<td>89.152674</td>
<td>2.564863</td>
</tr>
<tr>
<td>5</td>
<td>43</td>
<td>91.717537</td>
<td>0.515471</td>
</tr>
<tr>
<td>6</td>
<td>45</td>
<td>92.233008</td>
<td>0.993378</td>
</tr>
<tr>
<td>7</td>
<td>50</td>
<td>93.226386</td>
<td>0.980193</td>
</tr>
<tr>
<td>8</td>
<td>58</td>
<td>94.206579</td>
<td>0.370847</td>
</tr>
<tr>
<td>9</td>
<td>63</td>
<td>94.577426</td>
<td>0.331366</td>
</tr>
<tr>
<td>10</td>
<td>70</td>
<td>94.908792</td>
<td>0.034559</td>
</tr>
<tr>
<td>11</td>
<td>71</td>
<td>94.943351</td>
<td>0.160375</td>
</tr>
<tr>
<td>12</td>
<td>77</td>
<td>95.103726</td>
<td>0.020330</td>
</tr>
<tr>
<td>13</td>
<td>78</td>
<td>95.124057</td>
<td>0.127670</td>
</tr>
<tr>
<td>14</td>
<td>87</td>
<td>95.251726</td>
<td>0.034136</td>
</tr>
<tr>
<td>15</td>
<td>91</td>
<td>95.285863</td>
<td>0.007036</td>
</tr>
<tr>
<td>16</td>
<td>92</td>
<td>95.292899</td>
<td>0.018173</td>
</tr>
<tr>
<td>17</td>
<td>95</td>
<td>95.311072</td>
<td>0.014477</td>
</tr>
<tr>
<td>18</td>
<td>98</td>
<td>95.325549</td>
<td>0.020720</td>
</tr>
<tr>
<td>19</td>
<td>104</td>
<td>95.346268</td>
<td>0.002627</td>
</tr>
<tr>
<td>20</td>
<td>105</td>
<td>95.348895</td>
<td>0.018866</td>
</tr>
</tbody>
</table>
### TABLE III. DS2 - Successive differences of mean value function

<table>
<thead>
<tr>
<th>Failure Number</th>
<th>Time Between failures</th>
<th>m(t)</th>
<th>Successive Differences</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10</td>
<td>17.335844</td>
<td>13.002647</td>
</tr>
<tr>
<td>2</td>
<td>19</td>
<td>30.338491</td>
<td>15.233806</td>
</tr>
<tr>
<td>3</td>
<td>32</td>
<td>45.572296</td>
<td>10.235579</td>
</tr>
<tr>
<td>4</td>
<td>43</td>
<td>55.807875</td>
<td>10.898204</td>
</tr>
<tr>
<td>5</td>
<td>58</td>
<td>66.706079</td>
<td>6.723608</td>
</tr>
<tr>
<td>6</td>
<td>70</td>
<td>73.429688</td>
<td>7.587582</td>
</tr>
<tr>
<td>7</td>
<td>88</td>
<td>81.017270</td>
<td>4.602607</td>
</tr>
<tr>
<td>8</td>
<td>103</td>
<td>85.619877</td>
<td>4.755010</td>
</tr>
<tr>
<td>9</td>
<td>125</td>
<td>90.374887</td>
<td>3.452291</td>
</tr>
<tr>
<td>10</td>
<td>150</td>
<td>93.827178</td>
<td>1.714578</td>
</tr>
<tr>
<td>11</td>
<td>169</td>
<td>95.541757</td>
<td>1.707170</td>
</tr>
<tr>
<td>12</td>
<td>199</td>
<td>97.248926</td>
<td>1.007483</td>
</tr>
<tr>
<td>13</td>
<td>231</td>
<td>98.256409</td>
<td>0.453213</td>
</tr>
<tr>
<td>14</td>
<td>256</td>
<td>98.709623</td>
<td>0.394901</td>
</tr>
<tr>
<td>15</td>
<td>296</td>
<td>99.104523</td>
<td></td>
</tr>
</tbody>
</table>
V. CONCLUSION.

A number of estimates of software quality are based on the parameter estimates of SRGMs. Therefore, the quality estimates can be derived based on the quality estimates of parameters. In order to estimate the Software
reliability, a robust method of estimating parameter MGA is employed on Time domain software failure data. The graphs have shown out of control limits i.e below the LCL for DS1 and within control i.e between UCL and LCL for DS2. Hence we conclude that our method of estimation and the control chart are giving a +ve recommendation for their use in finding out preferable control process or desirable out of control signal. By observing the Failure Control chart we identified that the failure situation is detected at 10\textsuperscript{th} point of table-1 for the corresponding \( m(t) \), which is below \( m(t_{L}) \). The early detection of software failure will improve the software Reliability. When the time between failures is less than LCL, it is likely that there are assignable causes leading to significant process deterioration and it should be investigated. On the other hand, when the time between failures has exceeded the UCL, there are probably reasons that have led to significant improvement.

REFERENCES


Authors Profile:

Dr. R. Satya Prasad received Ph.D. degree in Computer Science in the faculty of Engineering in 2007 from Acharya Nagarjuna University, Andhra Pradesh. He received gold medal from Acharya Nagarjuna University for his outstanding performance in Masters Degree. He is currently working as Associate Professor in the Department of Computer Science & Engineering, Acharya Nagarjuna University. His current research is focused on Software Engineering. He has published 90 papers in National & International Journals.

Mrs. U. Usha Rani, Working as an Asst. Professor and Head in the Department of Computer Science and Engineering, Priyadarshini Engineering College, Chintalapudi, Tenali. She obtained her M.Sc. (Computer Science) degree from KSOU, Mysore, M.Tech. (CSE) from Acharya Nagarjuna University, Guntur. Her research interests lies in Software Engineering and Data Mining.
Dr. G. Krishna Mohan, working as Professor in the Department of Computer Science & Engineering, KL University. He obtained his M.C.A degree from Acharya Nagarjuna University, M.Tech(CSE) from Jawaharlal Nehru Technological University, Kakinada, M.Phil from Madurai Kamaraj University and Ph.D(CSE) from Acharya Nagarjuna University. He qualified, AP State Level Eligibility Test. His research interests lies in Data Mining and Software Engineering. He published 45 research papers in various National and International journals.